## **CHAPTER 13**

#### **Analysis of Variance: Factorial Designs**

#### Summary

A *factorial ANOVA* has one dependent variable and two or more independent variables called factors. Each level of one factor is paired with every level of the other factor. A factorial ANOVA tests three null hypotheses: one for each of the two independent variables and one for the interaction between the two independent variables.

Table 13.1 shows a 2 x 3 factorial design. Each participant receives one level of one independent variable and one level of the other independent variable. The participants in the upper left-hand cell of Table 13.1 get Level 1 of Factor A *and* Level 1 of Factor B. Their dependent-variable scores are entered into cell  $A_1B_1$ .

		In	dependent Variable	A	
		Level 1	Level 2	Level 3	Means
	Level 1	Participants'	Participants'	Participants'	$\overline{\mathbf{Y}}$
Independent		scores $(A_1B_1)$	scores $(A_2B_1)$	scores $(A_3B_1)$	$\bar{X}_{B_1}$
Variable B	Level 2	Participants'	Participants'	Participants'	$\overline{v}$
		scores $(A_1B_2)$	scores $(A_2B_2)$	scores $(A_3B_2)$	$\bar{X}_{B_2}$
	Means	$\bar{X}_{A_1}$	$\bar{X}_{A_2}$	$\bar{X}_{A_3}$	

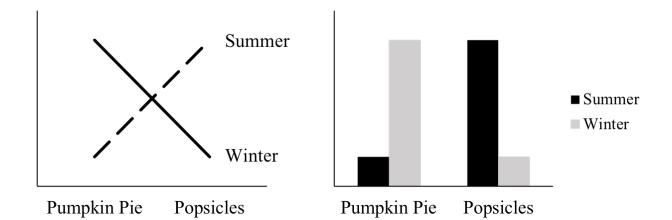
Table 13.1 Illustration of a 2 x 3 Factorial Design

Table 13.1 also shows marginal means for Factor A and marginal means for Factor B. The means for Factor A are used in *one* of the statistical tests that a factorial ANOVA produces, the main effect of Factor A. The marginal means for Factor B are involved in a *second* statistical test, the main effect of Factor B. Each *main effect* is comparable to a one-way ANOVA, and may be interpreted in the same way as a one-way ANOVA, unless the interaction is significant.

The *third test* in a factorial ANOVA is for an interaction between the two independent variables. *Interactions* occur when the effect of one independent variable depends upon which level of the other independent variable you are administering. That is, one independent variable influences the effect that a second independent variable has on the dependent variable.

Perhaps a concrete example of an interaction will help. Which type of dessert is more popular: pumpkin pie or popsicles? It is likely that the answer depends on the time of year. On a hot summer day, a popsicle might be more desirable than a warm slice of pumpkin pie; conversely, on a cold winter day, warm pie might be more appealing. The table and figures that follow present these results of a  $2 \times 2$  factorial design using various formats.

		Dessert Type (A)				
		Pumpkin Pie	Popsicles			
Time of Year	Summer	Low popularity	High popularity			
(B)	Winter	High popularity	Low popularity			



The effect of dessert type, then, depends on the time of year. In the summer, popsicles are preferred over pumpkin pie; in the winter, the opposite is true. Thus, an interaction is present.

A graph of the cell means is helpful when interpreting the results of a factorial ANOVA. A graph with lines that are not parallel *may* indicate that an interaction has occurred. Likewise, bar graphs with stair steps that change size or direction *may* indicate that two independent variables interact.

In conducting a two-way factorial ANOVA test, the total variability of all the scores is partitioned into four components. One component is the variability that is due to the first factor. A second component is the variability due to the second factor. A third component is the variability due to the interaction. The final component is the error variability, which serves as an estimate of the population variability. Each of these components, divided by its degrees of freedom, results in a mean square. The mean square for each main effect and the interaction is then divided by the error mean square to produce F values, which are then interpreted using a table of the sampling distribution of F.

Just as in the preceding chapters, *Tukey HSD* tests may be used to make pairwise comparisons among the levels of a factor. These tests can be conducted for either or for both of the factors in a factorial ANOVA. In Table 13.1, a Tukey HSD test on Factor B is unnecessary; the F test on that factor tells you whether or not the two marginal means are significantly different. Thus, Tukey HSD tests are only necessary if a factor has three or more levels. And, because main effects should be interpreted with caution when a significant interaction is present, only conduct Tukey HSD tests if the interaction is *not* significant. Similarly, estimates of effect size—both d and f—can be calculated as discussed in previous chapters, provided the interaction is not significant.

The *assumptions* introduced in Chapter 11 must be met by all data analyzed by ANOVA, including factorial ANOVA. These assumptions are that the dependent variable must be *normally distributed* in the populations from which the samples are drawn. The *variances* of the dependent variable must also be *equal* across each population. In addition to these assumptions, the methods described in Chapter 13 require that the *N*'s in each cell be equal, that the scores be independent (not paired or related), and that the levels of the independent variable be chosen by the experimenter rather than at random.

### **Multiple-Choice Questions**

1. As used in analysis of variance, the term factor means

- a. independent variable
- b. dependent variable
- c. extraneous variable
- d. none of the above

2. In terms of the number of factors present in a research design, which two tests are similar to one another?

- a. independent-samples *t* test and factorial ANOVA
- b. paired-samples t test and factorial ANOVA
- c. one-way ANOVA and factorial ANOVA
- d. none of the above

3. A social psychologist was interested in the effect of propaganda on attitudes of males and females. He measured attitudes toward democracy for all participants, delivered the propaganda, and re-measured attitudes toward democracy. He wanted to analyze the data using a 2 x 2 factorial with gender as one independent variable and timing of the attitude measure (before vs. after propaganda) as the other. The techniques presented in this chapter will not permit this because \_\_\_\_\_\_.

- a. the scores in each cell are not independent
- b. an independent variable was not included in the study
- c. the dependent variable was normally distributed
- d. the levels of the independent variable were not chosen at random by the experimenter

4. A cell in a factorial ANOVA refers to \_\_\_\_\_\_.

- a. one level of the independent variable
- b. one level of the dependent variable
- c. one level of one independent variable and one level of a second independent variable
- d. all the participants in the experiment

5. When the cell means of a factorial design are presented as a line graph, a nonsignificant interaction is indicated by

- a. parallel lines
- b. crossed lines
- c. values of F greater than 1.00
- d. all of the above

6. Suppose you had a 2 x 2 factorial ANOVA with the four cell means and you knew that *N* was 6 for each cell. With this information you could calculate \_\_\_\_\_\_.

- a.  $df_A$
- b.  $df_{AB}$
- c. *df*error
- d. all of the above

7. A 3 x 5 factorial ANOVA has \_\_\_\_\_\_ independent variables.

- a. 2
- b. 3
- c. 5
- d. 15

8. In a 4 x 4 factorial design with five scores per cell, the df for the interaction ( $F_{AB}$ ) would be \_\_\_\_\_.

- a. 3,70
- b. 6, 64
- c. 9,64
- d. none of the above

9. The term *main effect* refers to a comparison of \_\_\_\_\_\_.

- a. means for one factor
- b. interactions between factors
- c. both a. and b.
- d. neither a. nor b.

10. An interaction means that \_\_\_\_\_\_.

- a. the cell means all differed from one another
- b. the margin means for Factor A were identical
- c. there was a difference between two variables
- d. the effect of one factor depended on the level of the other factor

11. Researchers sometimes subtly expose participants to stimuli (a technique called *priming*) as a way to affect thoughts, feelings, or behaviors. Imagine researchers subtly exposed participants to either happy faces or sad faces (prime type), and then asked them to watch and rate their enjoyment of either a happy film clip or a sad film clip (film type). Which of the following statements would describe an interaction?

- a. Film type affected ratings of enjoyment, but prime type did not.
- b. Neither film type nor prime type affected ratings of enjoyment.
- c. Both film type and prime type affected ratings of enjoyment.
- d. Film type affected ratings of enjoyment, but only for those primed with sad faces.

12. "The means of the populations from which the samples were drawn are identical." This is a statement

- a. of a null hypothesis
- b. of one of the assumptions required of data analyzed with a factorial ANOVA
- c. about an interaction
- d. none of the above

13. Which of the following is (are) true?

- a.  $df_{\rm A} + df_{\rm B} = df_{\rm AB}$
- b.  $MS_{\rm A} + MS_{\rm B} = MS_{\rm AB}$
- c.  $SS_{cells} + SS_{error} = SS_{tot}$
- d. none of the above

14. Factorial ANOVA has which of the following assumptions in common with one-way ANOVA?

- a. the dependent variable is assumed to be normally distributed
- b. the variances of the dependent-variable scores are equal across populations
- c. both a. and b.
- d. neither a. nor b.

15. One difference between one-way ANOVA and factorial ANOVA is that factorial ANOVA

- a. has two or more dependent variables
- b. has one independent variable with more than 2 levels
- c. requires fewer assumptions about the data
- d. has two independent variables

16. Suppose a 5 x 6 factorial ANOVA with 7 scores per cell produced  $MS_A = 25$ ,  $MS_B = 30$ ,  $MS_{AB} = 15$ , and  $MS_{error} = 10$  (where Factor A has 5 levels and Factor B has 6 levels). At an alpha level of .01, a Tukey HSD

- a. is not appropriate in this instance
- b. would be significant for a difference of 2.00 between two Factor A means
- c. would be significant for a difference of 2.40 between two Factor A means
- d. none of the above

17. Suppose a 2 x 4 factorial ANOVA with 5 scores per cell produced  $MS_A = 200$ ,  $MS_B = 285$ ,  $MS_{AB} = 295$ , and  $MS_{error} = 100$  (where Factor A has 2 levels and Factor B has 4 levels). At an alpha level of .05, a Tukey HSD

- a. is not appropriate in this instance
- b. would be significant for a difference of 10 between two Factor B means
- c. would be significant for a difference of 15 between two Factor B means
- d. none of the above

18. Which of the following would be reason enough not to calculate effect size?

- a. a significant interaction
- b. a significant main effect
- c. either a. or b.
- d. neither a. nor b.

19. A follow-up Tukey HSD is not necessary for main effects when the *F* value is based on \_\_\_\_\_\_ degrees of freedom.

- a. 1, 20
- b. 2, 20
- c. 4, 20
- d. 4, 10

20. Consider a factorial ANOVA in which the dependent variable is reaction time scores. Three different drugs are tested on both females and males. The researchers concluded that the effect of a drug did not depend on whether a person taking it was a female or male. The factorial ANOVA would certainly show that \_\_\_\_\_\_.

- a. there is no main effect for drug
- b. there is no main effect for gender
- c. there is no interaction
- d. all of the above

#### Short Answer

1. Describe what a significant main effect tells us and what a significant interaction tells us.

2. In a factorial ANOVA design, when are Tukey HSD tests appropriate? When are they not appropriate?

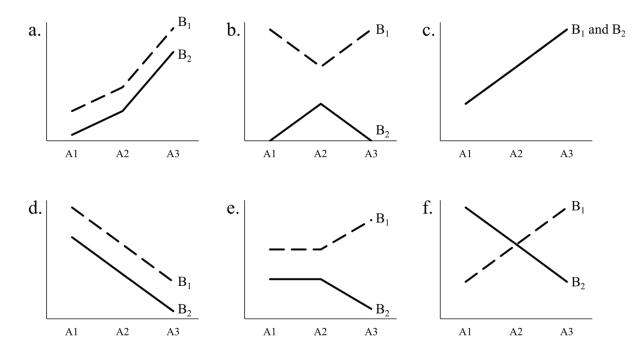
# Interpretations

1. The numbers below are cell means. For each set of means, indicate whether the interaction and the main effects are not significant or possibly significant.

	a.			
	$\mathbf{B}_1$	$B_2$	<b>B</b> <sub>3</sub>	
$A_1$	5	10	15	
$A_2$	5	10	15	
	b.			
	$B_1$	$B_2$	<b>B</b> <sub>3</sub>	
$egin{array}{c} A_1 \ A_2 \end{array}$	15	10	15	
$A_2$	5	10	5	

	с.	
	$B_1$	$B_2$
$A_1$	5	10
A <sub>2</sub>	10	5
	d.	
	$B_1$	$B_2$
$A_1$	5	10
$A_1 \\ A_2$	5	10
(	e.	
	$B_1$	$B_2$
$A_1$	5	5
$A_2$	5	10

2. For each figure, indicate whether the interaction and the main effects are not significant or possibly significant.



3. Across five studies, Makhanova, McNulty, and Maner (2017) researched the psychology of selfies. In Study 2, they examined whether the gender of the person taking the selfie and the gender of the people who would view the selfie would influence the angle at which the photograph was taken. They predicted that women would be more likely to take selfies from a downward angle, which would make them appear smaller, whereas men would be more likely to take selfies from an upward angle, which would make them appear larger. Research assistants approached students on a college campus and asked each of them to take a picture of themselves on a provided camera. Before taking the picture, participants were told that their photo would be shown to either same-gender or other-gender viewers (men for women; women for men). The research assistants coded the angle at which the selfies were taken using a scale ranging from -2 (holding the camera far below the face; low, upward angle) to +2 (holding the camera far above the face; high, downward angle), with 0 representing holding the camera at eye level. Below are modified summary data from Study 2 of Makhanova et al. (2017; retrieved from <a href="https://osf.io/edx28/">https://osf.io/edx28/</a> on July 14, 2018). Set alpha at .05 and find the appropriate critical values. Use the data to write a paragraph summarizing the findings.

•		Same gender	Women e gender -0.16 gender 0.27		Gender (A) Men -0.45 0.05		$\bar{X}_{B1} = -0.31$ $\bar{X}_{B2} = 0.16$	
			$\overline{X}_{A1}=0.$	05	$\overline{X}_{A2} = \cdot$	-0.20		
_	Source		SS	df	MS	F	d	
	Particip	ant Gender (A)	3.95	1	3.95	4.25	0.26	
	Viewer	Gender (B)	13.21	1	13.21	14.20	0.49	
	AB Inte	raction	0.06	1	0.06	0.06		
	Error		229.63	246	0.93			
-	TOTAL		245.85	249				

### Problems

1. In a series of studies, O'Brien and Roney (2017) studied people's predictions about and actual experiences of enjoyment of leisure tasks performed before or after completing a work task. In their second study, participants were given descriptions of two tasks: one leisure task (called the *Magic Maker* task) and one tedious task (called the *Fixed Labor* task). Half of the participants actually completed both tasks ("experiencers") and half of the participants only imagined completing both tasks ("predictors"). Additionally, half of the participants played (or imagined playing) the leisure task first and half of the participants played (or imagined playing) the leisure task second. The dependent variable was how much participants rated their experienced or predicted enjoyment of playing *Magic Maker*. Below are modified summary data from Study 2 of O'Brien and Roney (2017; retrieved from <a href="https://osf.io/xmnyq/">https://osf.io/xmnyq/</a> on July 13, 2018) that will allow you to closely replicate the results. Conduct a factorial ANOVA test—including Tukey HSD tests and estimates of effect size, if appropriate—and write a paragraph summarizing the findings. Set alpha at .05.

*Note.* Because sample sizes in the original data set were unequal across cells, participants' data were dropped at random in three out of four conditions for the purposes of the calculations.

		Factor A: Role				
		Experiencer (A <sub>1</sub> )	Predictor (A <sub>2</sub> )			
		$\Sigma X_{A1B1} = 117.67$	$\Sigma X_{A2B1} = 46.00$			
Factor B: Task Order	Leisure First (B1)	$\Sigma X^2_{A1B1} = 441.89$	$\Sigma X^2_{A2BI} = 246.44$			
		N = 40	N = 40			
		$\Sigma X_{A1B2} = 121.00$	$\Sigma X_{A2B2} = 113.33$			
	Leisure Second (B <sub>2</sub> )	$\Sigma X^2_{A1B2} = 545.89$	$\Sigma X^2_{A2B2} = 442.00$			
		N = 40	N = 40			

2. Maglio and Polman (2014) studied the effects of spatial orientation on estimates of psychological distance. In their second study, researchers approached people at a subway station in Toronto, Ontario who were either on the eastbound platform (headed toward the University of Toronto campus) or the westbound platform (heading away from the University of Toronto campus). Researchers then asked each participant to either face toward or away from the University of Toronto and rate how far away they were from the campus on a scale of 1 (very close) to 7 (very far). Below are summary data from Study 2 of Maglio and Polman (2014; retrieved from https://osf.io/7rajd/ on July 13, 2018) that will allow you to replicate the results. Conduct a factorial ANOVA test-including Tukey HSD tests and estimates of effect size, if appropriate—and write a paragraph summarizing the findings. Set alpha at .05.

		Factor A: Direction Traveling			
	_	Toward Campus (A1)	Away from Campus (A <sub>2</sub> )		
		$\Sigma X_{AIBI} = 73$	$\Sigma X_{A2BI} = 86$		
	Toward Campus (B1)	$\Sigma X^2_{A1B1} = 285$	$\Sigma X^2_{A2B1} = 396$		
Factor B:		N = 20	N = 20		
Direction Facing		$\Sigma X_{A1B2} = 72$	$\Sigma X_{A2B2} = 80$		
	Away from Campus (B <sub>2</sub> )	$\Sigma X^2_{A1B2} = 280$	$\Sigma X^2_{A2B2} = 342$		
		N = 20	N = 20		

Factor	: A:	Direc	tion Tr	avelin	g	

## ANSWERS

### **Multiple-Choice Questions**

- 1. a
- 2. d

**Explanation:** A factorial ANOVA design involves two independent variables (factors), whereas independent-samples *t* tests, paired-samples *t* tests, and one-way ANOVA designs all involve only one independent variable.

3. a

**Explanation:** In this design, one of the factors (timing of the attitude measure) was a repeated measure. The techniques presented in Chapter 13 require that all observations be independent of one another.

4. c

- 5. a
- 6. d
- 7. a

**Explanation:** This notation tells you that there are two independent variables. The first independent variable has three levels and the second independent variable has five levels. There are 15 different cells in this design, but only two independent variables.

8. c

**Explanation:** The first df is for the interaction term and the second df is for the error term.  $N_{\text{tot}}$  is found by multiplying the number of scores per cell (5) by the number of cells (16).

- 9. a
- 10. d
- 11. d

**Explanation:** Response option a. describes a main effect of film type, with no main effect of prime type. Response options b. and c. describe no main effects and two main effects, respectively. Option d. describes an effect of film type that *depends on* the level of prime type. An interaction occurs when the effect of one factor depends on the level of another factor.

12. a

### 13. c

- 14. c
- 15. d
- 16. c

**Explanation:** Because the interaction is not significant ( $F_{AB} = 1.50$ , p > .01), Tukey HSD tests *are* permissible. With  $s_{\bar{X}} = \sqrt{\frac{MS_{error}}{N_t}} = \sqrt{\frac{10}{42}} = 0.49$ , a mean difference of 2.00 results in an HSD value of 4.08 and a mean difference of 2.40 results in an HSD value of 4.90. The critical HSD value for  $df_{error} = 180$  (use 120 in Table G) and 5 levels of Factor A is 4.71. Thus, a mean difference 0 2.00 is not significant, but a mean difference 2.40 is significant. Note that  $N_t$  is equal to the total number of scores at one level of A, which would be the sample size of one cell (7) multiplied by the number of rows (6).

17. a

**Explanation:** Because the interaction is significant ( $F_{AB} = 2.95$ , p < .05), Tukey HSD tests are not appropriate to conduct.

18. a

**Explanation:** When a significant interaction is present, interpretation of main effects is typically not recommended.

19. a

**Explanation:** The df for the numerator is 1 when a factor has only two levels. When a factor has only two levels, the F test alone tells you about the difference between the two means.

20. c

**Explanation:** When the effect of one independent variable *does not depend* on the level of the second independent variable, an interaction is not present. There is not enough information to determine the possible significance of main effects in this question.

## Short Answer

1. A significant main effect indicates mean levels of *one* independent variable significantly differ from the grand mean. In other words, a significance test for a main effect tells us the probability of the means from every level of one factor coming from the same population. If p < .05, then it's unlikely all means for one factor came from the same population. With significant interactions, however, it is necessary to talk about the *joint effect* of two or more independent variables. In other words, a significant interaction indicates that

the effect of one factor *depends* on the effect of another factor.

2. Tukey HSD tests are appropriate to calculate in factorial designs when you have a significant main effect for a factor that has more than two levels. If a factor has only two levels, a Tukey HSD test is not necessary. If a significant interaction is present, Tukey HSD tests are not appropriate to calculate.

### Interpretations

1.

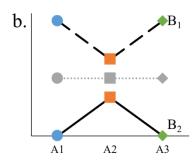
- a. AB interaction: not significant; Main effect of A: not significant; Main effect of B: possibly significant
- b. AB interaction: possibly significant; Main effect of A: possibly significant; Main effect of B: not significant
- c. AB interaction: possibly significant; Main effect of A: not significant; Main effect of B: not significant
- d. AB interaction: not significant; Main effect of A: not significant; Main effect of B: possibly significant
- e. AB interaction: possibly significant; Main effect of A: possibly significant; Main effect of B: possibly significant

A helpful strategy when answering questions like these is to actually graph the data. Plot one factor on the *x*-axis, the scores on the *y*-axis, and represent the other factor with different lines or patterns. With a line graph, you can make inferences about interactions based on whether the lines are parallel (no significant interaction) or not parallel (possible significant interaction). For inferences about main effects, it's often easiest to look at means. Using part a. of this question as an example, the mean for  $A_1$  is 10 ([5 + 10 + 15] / 3) and the mean for  $A_2$  is 10. These means are identical, so there is no main effect of Factor A. The mean for  $B_1$  is 5, the mean for  $B_2$  is 10, and the mean for  $B_3$  is 15. These means are different from one another, so a main effect of Factor B is possible.

#### 2.

- a. AB interaction: not significant; Main effect of A: possibly significant; Main effect of B: possibly significant
- b. AB interaction: possibly significant; Main effect of A: not significant; Main effect of B: possibly significant
- c. AB interaction: not significant; Main effect of A: possibly significant; Main effect of B: not significant
- d. AB interaction: not significant; Main effect of A: possibly significant; Main effect of B: possibly significant
- e. AB interaction: possibly significant; Main effect of A: not significant; Main effect of B: possibly significant
- f. AB interaction: possibly significant; Main effect of A: not significant; Main effect of B: not significant

With a line graph, you can make inferences about interactions based on whether the lines are parallel (no significant interaction) or not parallel (possible significant interaction). Inferences about main effects can sometimes be harder to spot. Using part b. of this question as an example, a main effect of Factor B is possibly significant because the entire line for  $B_1$  (and, thus, the overall mean for  $B_1$ ) is higher than the entire line for  $B_2$ . The nonsignificant main effect of A can be harder to spot. In graph that follows, the cell means for  $A_1$  are represented by blue circles, the cell means for  $A_2$  are represented by orange squares, and the cell means for  $A_3$  are represented by green diamonds. If you were to visually approximate the mean of both blue circles, the mean of both orange squares, and the mean of both green diamonds, you would get the gray markers in the middle of the graph, which are all at the same level. Because they are at the same level, there is no main effect of Factor A present.



### 3. Critical values: $F_{.05}(1, 200) = 3.89$ (same for all three tests)

The interaction between the gender of the participant and the gender of the viewer was not significant (p > .05). However, the main effect of the gender of the participant was significant (p < .05). On average, women took their photos at higher, more downward angles, whereas men took their photos at lower, more upward angles. The effect size index for this difference, d = 0.26, was small. The main effect of the gender of the viewers was also significant (p < .05). On average, participants who believed their photo would be viewed by members of a different gender took their photos at higher, more downward angles, whereas participants who believed their photos at lower as participants who believed their photos at lower at lower, more upward angles. The effect size index for this difference, d = 0.49, was medium.

APA format: A 2 (gender of the participant: women vs. men) x 2 (gender of the viewer: same gender vs. other gender) factorial ANOVA was conducted to test the effects of gender on the angle at which selfies are taken. There was no significant interaction between gender of the participant and gender of the viewer on photograph angles, F(1, 246) = 0.06, p > .05. However, there were significant main effects of participant gender, F(1, 246) = 4.25, p < .05, d = 0.26, and viewer gender, F(1, 246) = 14.20, p < .05, d = 0.49. On average, the angle of the photographs were higher (more downward) both when taken by women (M = 0.05) and when taken for other-gender viewers (M = 0.16). This is in contrast to the average angle of photographs taken by men (M = -0.20) and for same-gender viewers (M = -0.31), which tended to be lower (more upward). The magnitude of these effects were small and medium, respectively. Thus, how people take selfies depends more on the gender of who will view the photo than the gender of who is taking the photo.

For this problem, note that Table F in the textbook does not provide a critical value for df = 1, 246. When that happens, always use the next lowest df option, which is df = 1, 200 for this problem. Although we used the critical value associated with df = 1, 200, report the actual df in the APA-formatted conclusion. Additionally, because each factor has only two levels, Tukey HSD tests were not necessary or provided.

#### Problems

1.

Source	SS	df	MS	F	р
Role (A)	39.34	1	39.34	10.41	< .05
Task Order (B)	31.20	1	31.20	8.25	< .05
AB Interaction	25.28	1	25.28	6.69	< .05
Error	590.05	156	3.78		
TOTAL	686.20	159			

There was a significant interaction between the role the participant played and which task came first on ratings of task enjoyment (p < .05). In other words, the effect of the order of the task on task enjoyment *depended on* whether the participants actually completed the tasks or not. For those who only imagined completing the tasks, average ratings of expected enjoyment were lower when the leisure task came before a work task than when it came after a work task. For those who actually completed both tasks, though,

average ratings of experienced enjoyment were very similar between the two task orders. Thus, although people may expect to enjoy leisure tasks less when a work task remains undone, in actual experience, leisure tasks are similarly enjoyable both before and after work. There were also significant main effects of role of the participant (p < .05) and task order (p < .05), but further interpretation of the main effects is not recommended because of the presence of a significant interaction that is primarily driven by one cell.

APA format: A 2 (role: experiencer vs. predictor) x 2 (task order: leisure first vs. leisure second) factorial ANOVA was conducted to examine perceived and experienced enjoyment of a leisure activity that came either before or after a work task. There were significant main effects for both role, F(1, 156) = 10.41, p < .05, and task order, F(1, 156) = 8.25, p < .05. These main effects were qualified by a significant interaction between the two factors, F(1, 156) = 6.69, p > .05. For those who only imagined completing the tasks, average ratings of expected enjoyment were lower when the leisure task came before a work task than when it followed a work task. For those who actually completed both tasks, though, average ratings of experienced enjoyment were very similar between the two task orders. Thus, although people may expect to enjoy leisure tasks less when a work task remains undone, in actual experience, leisure tasks are similarly enjoyable both before and after work.

Task Order (B)  
Leisure First  
Leisure Second  

$$\frac{Experiencer}{3.03} = \frac{Predictor}{2.94} = \frac{Predictor}{3.03} = \frac{1.15}{X_{B2}} = 2.93 \\ \overline{X}_{A1} = 2.98 \\ \overline{X}_{A2} = 1.99 \\ \overline{X}_{A3} = 1.99 \\ \overline{X}_{$$

Check:  $SS_{AB} = 96.15 - 39.34 - 31.20 = 25.61$ 

\*Note: Because of rounding errors, your calculations for  $SS_{AB}$  don't perfectly match. Use 25.61 in your ANOVA table.

$$SS_{error} = \sum \left[ \sum_{cell} X_{cell}^{2} - \frac{(\sum_{cell} X_{cell})^{2}}{N_{cell}} \right]$$
  
=  $\left[ 441.89 - \frac{(117.67)^{2}}{40} \right] + \left[ 246.44 - \frac{(46)^{2}}{40} \right] + \left[ 545.89 - \frac{(121)^{2}}{40} \right] + \left[ 442 - \frac{(113.33)^{2}}{40} \right]$   
=  $\left[ 95.734 \right] + \left[ 193.54 \right] + \left[ 179.865 \right] + \left[ 120.908 \right] = 590.05$ 

Check:  $SS_{total} = 96.15 + 590.05 = 686.20$ 

$$\begin{aligned} df_{tot} &= N_{tot} - 1 = 160 - 1 = 159 \\ df_{role} &= A - 1 = 2 - 1 = 1 \\ df_{task \ order} &= B - 1 = 2 - 1 = 1 \\ df_{AB} &= (A - 1)(B - 1) = (1)(1) = 1 \\ df_{error} &= N_{tot} - (A)(B) = 160 - (2)(2) = 156 \end{aligned}$$

$$MS_{role} = \frac{SS_{role}}{df_{role}} = \frac{39.34}{1} = 39.34$$

$$MS_{task \ order} = \frac{SS_{task \ order}}{df_{task \ order}} = \frac{31.20}{1} = 31.20$$

$$MS_{AB} = \frac{SS_{AB}}{df_{AB}} = \frac{25.28}{1} = 25.28$$

$$MS_{error} = \frac{SS_{error}}{df_{error}} = \frac{590.05}{156} = 3.78$$

$$F_{role} = \frac{MS_{role}}{MS_{error}} = \frac{39.34}{3.78} = 10.41$$

$$F_{task \ order} = \frac{MS_{task \ order}}{MS_{error}} = \frac{31.20}{3.78} = 8.25$$

$$F_{AB} = \frac{MS_{AB}}{MS_{error}} = \frac{25.28}{3.78} = 6.69$$

For this problem, note that Table F in the textbook does not provide a critical value for df = 1, 156. When that happens, always use the next lowest df option, which is df = 1, 150 for this problem. Although we used the critical value associated with df = 1, 150, report the actual df in the APA-formatted conclusion. Additionally, because the interaction was significant and each factor has only two levels, Tukey HSD tests and estimates of effect size are not appropriate. And, because the significant interaction was driven largely by one cell (predictors with the leisure task first), further interpretation of the main effects is not recommended.

Source	SS	df	MS	F	р
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2.

Direction Traveling (A)	5.52	1	5.52	4.80	<.05
Direction Facing (B)	0.61	1	0.61	0.53	> .05
AB Interaction	0.31	1	0.31	0.27	>.05
Error	87.55	76	1.15		
TOTAL	93.99	79			

The interaction between the direction participants were traveling and the direction they were facing when estimating the distance of the University of Toronto was not significant (p > .05). The main effect of what direction they were facing was also not significant (p > .05). However, the direction participants were traveling did have a significant effect on their estimates of distance. Those traveling *toward* the University of Toronto campus estimated the campus to be closer to the subway station than those traveling *away* from the campus (p < .05). The effect size index, d = 0.48, indicates a medium effect.

APA format: A 2 (direction traveling: away vs. toward) x 2 (direction facing: away vs. toward) factorial ANOVA was conducted to test the effects of spatial (direction traveling) and visual (direction facing) orientation on estimates of subjective distance. There was no significant interaction between direction traveling and direction facing on estimates of subjective difference, F(1, 76) = 0.27, p > .05, nor was there a significant main effect of direction facing, F(1, 76) = 0.53, d = 0.17, p > .05. However, there was a significant main effect of direction traveling, F(1, 76) = 4.79, d = 0.48, p < .05, such that those traveling toward the campus estimated the campus to be closer (M = 3.63) than those traveling away from the campus (M = 4.15). The magnitude of this main effect was medium.

		Direction 7	Fraveling (A)			
		Toward	Away from			
		Campus	Campus	_		
Direction	Toward Campus	3.65	4.30	$\bar{X}_{B1} = 3.98$		
Facing (B)	Away from Campus	3.60	4.00	$\bar{X}_{B2} = 3.80$		
		$\bar{X}_{A1} = 3.63$	$\bar{X}_{A2} = 4.15$	$\bar{X}_{GM} = 3.89$		
$SS_{tot} = \sum_{i=1}^{2} X_{tot}^{2} - \frac{(\sum_{i=1}^{2} X_{tot})^{2}}{N_{tot}} = 1,303 - \frac{(311)^{2}}{80}$ $= 1,303 - 1,209.0125 = 93.99$ $SS_{cells} = \sum_{i=1}^{2} \left[ \frac{(\sum_{i=1}^{2} X_{cell})^{2}}{N_{cell}} \right] - \frac{(\sum_{i=1}^{2} X_{tot})^{2}}{N_{tot}}$ $= \left[ \frac{(73)^{2}}{20} \right] + \left[ \frac{(86)^{2}}{20} \right] + \left[ \frac{(72)^{2}}{20} \right] + \left[ \frac{(80)^{2}}{20} \right] - \frac{(311)^{2}}{80}$						
$= 266.45 + 369.8 + 259.2 + 320 - 1,209.013 = 6.44$ $SS_{traveling} = \sum_{n=1}^{\infty} \left[ \frac{(\sum X_A)^2}{N_A} \right] - \frac{(\sum X_{tot})^2}{N_{tot}}$ $= \left[ \frac{(145)^2}{40} \right] + \left[ \frac{(166)^2}{40} \right] - \frac{(311)^2}{80}$ $= 525.63 + 688.9 - 1,209.013 = 5.52$						
$=$ $\left[\frac{(}{-}\right]$	$\frac{159)^2}{40} - \frac{(\sum X_{bol})^2}{N_{bol}} - \frac{(\sum X_{tot})^2}{N_{tot}} + \frac{(152)^2}{40} - \frac{(32)^2}{40} - \frac{(32)^2}{40} + \frac{(152)^2}{40} - \frac{(32)^2}{40} + \frac{(152)^2}{40} - \frac{(32)^2}{40} + \frac$	$\frac{(311)^2}{80}$				

$$SS_{AB} = N_{cell} \sum \left[ (\bar{X}_{AB} - \bar{X}_A - \bar{X}_B + \bar{X}_{GM})^2 \right]$$
  
= 20  $\begin{bmatrix} (3.65 - 3.63 - 3.98 + 3.89)^2 + (4.30 - 4.15 - 3.98 + 3.89)^2 \\ + (3.60 - 3.63 - 3.80 + 3.89)^2 + (4.00 - 4.15 - 3.80 + 3.89)^2 \end{bmatrix}$   
= 20[(-0.07)<sup>2</sup> + (0.06)<sup>2</sup> + (0.06)<sup>2</sup> + (-0.06)<sup>2</sup>] = 20(0.0157) = 0.31

Check:  $SS_{AB} = 6.44 - 5.52 - 0.61 = 0.31$ 

$$SS_{error} = \sum \left[ \sum_{cell} X_{cell}^{2} - \frac{(\sum_{cell} X_{cell})^{2}}{N_{cell}} \right]$$
  
=  $\left[ 285 - \frac{(73)^{2}}{20} \right] + \left[ 396 - \frac{(86)^{2}}{20} \right] + \left[ 280 - \frac{(72)^{2}}{20} \right] + \left[ 342 - \frac{(80)^{2}}{20} \right]$   
=  $[18.55] + [26.2] + [20.8] + [22] = 87.55$ 

Check:  $SS_{total} = 6.44 + 87.55 = 93.99$ 

$$\begin{aligned} df_{tot} &= N_{tot} - 1 = 80 - 1 = 79 \\ df_{traveling} &= A - 1 = 2 - 1 = 1 \\ df_{facing} &= B - 1 = 2 - 1 = 1 \\ df_{AB} &= (A - 1)(B - 1) = (1)(1) = 1 \\ df_{error} &= N_{tot} - (A)(B) = 80 - (2)(2) = 76 \end{aligned}$$

$$MS_{traveling} = \frac{SS_{traveling}}{df_{traveling}} = \frac{5.52}{1} = 5.52$$

$$MS_{facing} = \frac{SS_{facing}}{df_{facing}} = \frac{0.61}{1} = 0.61$$

$$MS_{AB} = \frac{SS_{AB}}{df_{AB}} = \frac{0.31}{1} = 0.31$$

$$MS_{error} = \frac{SS_{error}}{df_{error}} = \frac{87.55}{76} = 1.15$$

$$F_{traveling} = \frac{MS_{traveling}}{MS_{error}} = \frac{5.52}{1.15} = 4.80$$

$$F_{facing} = \frac{MS_{facing}}{MS_{error}} = \frac{0.61}{1.15} = 0.53$$

$$F_{AB} = \frac{MS_{AB}}{MS_{error}} = \frac{0.31}{1.15} = 0.27$$

$$d_{traveling} = \frac{\bar{X}_1 - \bar{X}_2}{\hat{s}_{error}} = \frac{3.63 - 4.15}{\sqrt{1.15}} = |-0.48|$$

$$d_{facing} = \frac{\bar{X}_1 - \bar{X}_2}{\hat{s}_{error}} = \frac{3.98 - 3.80}{\sqrt{1.15}} = 0.17$$

Critical values:  $F_{.05}(1, 70) = 3.98$  (same for all three tests)

For this problem, note that Table F in the textbook does not provide a critical value for df = 1, 76. When that happens, always use the next lowest df option, which is df = 1, 70 for this problem. Although we used the critical value associated with df = 1, 70, report the actual df in the APA-formatted conclusion. Additionally, because each factor has only two levels, Tukey HSD tests are not appropriate.

## References

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